

## SOLIDS SEPARATION

Sedimentation and clarification are used interchangeably for potable water; both refer to the separating of solid material from water.

Since most solids have a specific gravity greater than 1, gravity settling is used to remove suspended particles. When specific gravity is less than 1, floatation is normally used.

1. various types of sedimentation exist, based on characteristics of particles
  - a. *discrete or type 1 settling*; particles whose size, shape, and specific gravity do not change over time
  - b. *flocculating particles or type 2 settling*; particles that change size, shape and perhaps specific gravity over time
  - c. type 3 (hindered settling) and type IV (compression); not used here because mostly in wastewater
2. above types have both dilute and concentrated suspensions
  - a. dilute; number of particles is insufficient to cause displacement of water (most potable water sources)
  - b. concentrated; number of particles is such that water is displaced (most wastewaters)
3. many applications in preparation of potable water as it can remove:
  - a. suspended solids
  - b. dissolved solids that are precipitated

Examples:

- ▶ plain settling of surface water prior to treatment by rapid sand filtration (type 1)
- ▶ settling of coagulated and flocculated waters (type 2)
- ▶ settling of coagulated and flocculated waters in lime-soda softening (type 2)
- ▶ settling of waters treated for iron and manganese content (type 1)

## Ideal Settling Basin (rectangular)

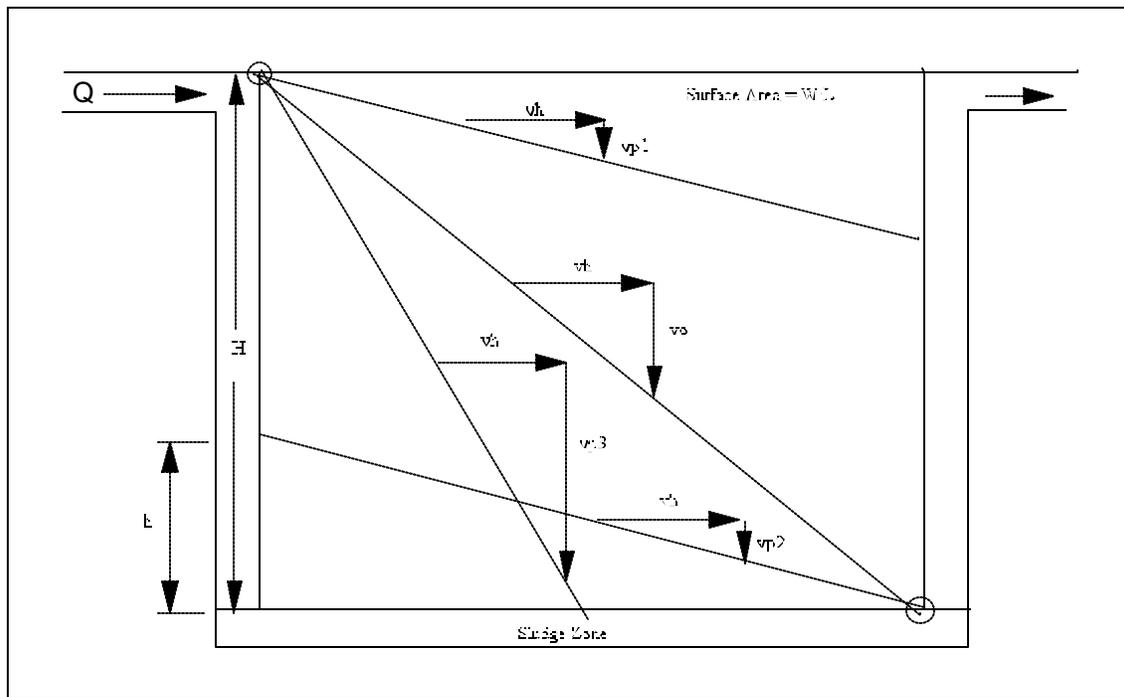
- ▶ steady flow conditions (constant flow at a constant rate)
- ▶ settling in sedimentation basin is ideal for discrete particles
- ▶ concentration of suspended particles is same at all depths in the inlet zone
- ▶ once a particle hits the sludge zone it stays there
- ▶ flow through period is equal to detention time

$L =$  length of basin  $v_h =$  horizontal velocity of flow

$v_{pi} =$  settling velocity of any particle  $W =$  width of basin

$H =$  height of basin

$v_o =$  settling velocity of the smallest particle that has 100 % removal



**Figure 1: Ideal Settling Basin**

▶ particle entering at Point 1 has a trajectory as shown to intercept the sludge zone at Point 2

▶ vertical detention time,  $t_v$  = depth of tank / ideal settling velocity

$$t_v = \frac{H}{v_o} \quad (1)$$

▶ horizontal detention time also equals flow through velocity,  $v_h$

$$t_h = \frac{L}{v_h} \quad (2)$$

where

$$v_h = \frac{Q}{H \cdot W} \quad (3)$$

thus

$$t_h = \frac{L \cdot W \cdot H}{Q} \quad (4)$$

▶ equating t's

$$\frac{L \cdot W \cdot H}{Q} = \frac{H}{v_o} \quad (5)$$

or

$$v_o = \frac{Q}{L \cdot W} \quad (6)$$

or

$$v_o = \frac{Q}{A_p} \quad (7)$$

where

$A_p$  = is the plan area of the settling basin

$v_o$  = overflow rate at which 100 % of the given particles are removed

### ***Ideal Settling Basin (circular)***

▶ same principals as for rectangular apply

▶ try solving it as an example problem



Overflow expression (Eq. 7) shows that settling is independent of depth

- ▶ provided for
  - ▶ sludge bed depth
  - ▶ rakes
  - ▶ resuspension
  - ▶ scouring
  - ▶ wind turbulence
- ▶ fractional removal as not all particles have settling velocity of  $v_o$ 
  - ▶ faster ones ( $v_p > v_o$ ) will settle out as they intercept sludge
  - ▶ slower ones ( $v_p < v_o$ ) will not settle out
  - ▶ fractional removal (R)

$$R = \frac{h}{H} = \frac{v_p}{v_o} \quad (8)$$

#### Design Data

- ▶ rectangular
  - ▶ depth: 3-5 m
  - ▶ length: 15-90 m
  - ▶ width: 3-24 m
- ▶ circular
  - ▶ depth: 3-5 m
  - ▶ diameter: 4-60 m

#### Type 1 Settling

- ▶ discrete settling of individual particles
  - ▶ plain sedimentation

#### *Theoretical(Terminal Settling)* STUDENTS RESPONSIBLE

- ▶ easiest situation to analyze as based on fluid mechanics
- ▶ particle suspended in water has initially two forces acting on it

(1) gravity  $\Rightarrow f_g = \rho_p g V_p$

where

- $\rho_p$  = particle density
- $g$  = gravitational constant

$V_p$  = volume of the particle

$$(2) \quad \text{buoyancy } f_b = \rho_w g V_p$$

where

$\rho_w$  = density of water

Since these forces are in opposite directions, there will be net force or movement. However, if the density of the particle is different than that for water, the particle will accelerate in the direction of the force:

$$f_{\text{net}} = (\rho_p - \rho_w) g V_p$$

This net force causes acceleration

Once motion is initiated, a third force acts on the particle, drag.

$$f_d = (1/2) C_D A_p \rho_w v^2$$

where

$C_D$  = drag coefficient

$A_p$  = cross-sectional area of particle perpendicular to direction of movement

$v$  = velocity

Acceleration continues at a decreasing rate until a steady velocity is attained, ie. drag force equals driving force:

$$(\rho_p - \rho_w) g V_p = (1/2) C_D A_p \rho_w v^2$$

For spherical particles it can be shown that:

$$V_p/A_p = (2/3)d$$

Using in above equation:

$$v_t^2 = (4/3)g[(\rho_p - \rho_w)d/C_D\rho_w]$$

Expressions for  $C_D$  change with flow regimes:

$$C_D = 24/R_e \quad \textit{laminar} \quad Re < 1$$

$$C_D = 24/R_e + 3/R_e^{0.5} + 0.34 \quad \textit{transitional} \quad 10^3 > Re > 1$$

$$C_D = 0.4 \quad \textit{turbulent} \quad Re > 10^3$$

$$R_e = \phi v_t \rho_w d / u$$

where

$\phi$  = shape factor, 1.0 for perfect spheres

$u$  = dynamic viscosity of fluid

To determine terminal settling velocity, above equations must be solved simultaneously.

## Non-Theoretical

- ▶ fractional removal determined by method developed by Camp 1946
- ▶ suspension is placed in column and completely mixed and then allowed to settle quiescently

Particle placed at the surface has an *average* settling velocity of:

$$v_o = \text{distance travelled}/\text{time of travel} \\ = Z_o/t_o$$

Another particle placed at distance  $Z_p$ , terminal velocity less than the surface particle, but arrives at the same time, has a settling velocity of:

$$v_p = Z_p/t_o$$

which is  $< v_o$ ; but arrives at sampling port a same time

Thus, the travel time for both particles is equal, where

$$t_o = Z_o/v_o = Z_p/v_p \quad \text{and} \quad v_p/v_o = Z_p/Z_o = h/H$$

Thus some generalized statements can be made concerning the above relationships.

1. All particles having a diameter equal to or greater than  $d_o$ , i.e. have settling velocity greater than  $v_o$ , will arrive at or pass the sampling port in time  $t_o$ . (*Assume equal  $S_s$* )
2. article with diameter  $d_p < d_o$  will have a settling  $v_p < v_o$ , will arrive at or pass the sampling port in time  $t_o$ , provided its position is below  $Z_p$ .
3. If the suspension is uniformly mixed, i.e. particles are randomly distributed, then the fraction of particles with size  $d_p$  having settling velocity  $v_p$  which will arrive at or pass the sampling port in time  $t_o$  will be  $Z_p/Z_o = v_p/v_o$ . Thus the removal efficiency of any size particle from suspension is the ratio of the settling velocity of that particle to the settling velocity  $v_o$  defined as  $Z_p/Z_o$ .

These principles can be used to determine the settleability of any given suspension, using shown apparatus. Theoretically depth is not a factor but for practical reasons, 2 m is usually chosen.

### Procedure:

- 1) Determine  $C_o$  of completely mixed suspension at time zero.
- 2) Measure  $C_1$  at time  $t_1$ . All particles comprising  $C_1$  have a settling velocity less than  $Z_o/t_1$ , where  $v_1 = Z_o/t_1$ . Thus, the mass fraction of particles removed with  $v_1 < Z_o/t_1$  is given by  $r_1 = C_1/C_o$ .
- 3) Repeat process with several times  $t_i$ , with the mass fraction of particles being  $v_i < Z_o/t_i$
- 4) Values are then plotted on a graph to obtain Figure 3, where the fraction of particles remaining for any settling velocity can be determined
- 5) For any detention time  $t_o$ , an overall percent removal ( $r_o$ ) can be obtained. That is, all particles having a settling velocity greater that  $v_o = Z_o/t_o$ , will be removed 100% (un-hatched area in Figure 3;  $1 - r_o$ ). The remaining particles have a  $v_i < v_o$  (hatched area in Figure 1), and will be removed according to ratio  $v_i/v_o$ .

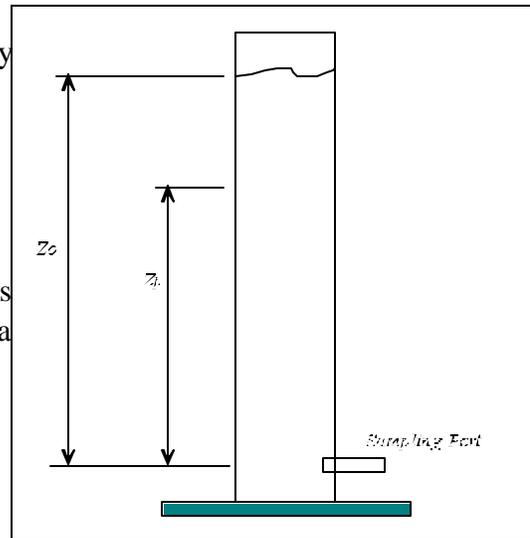
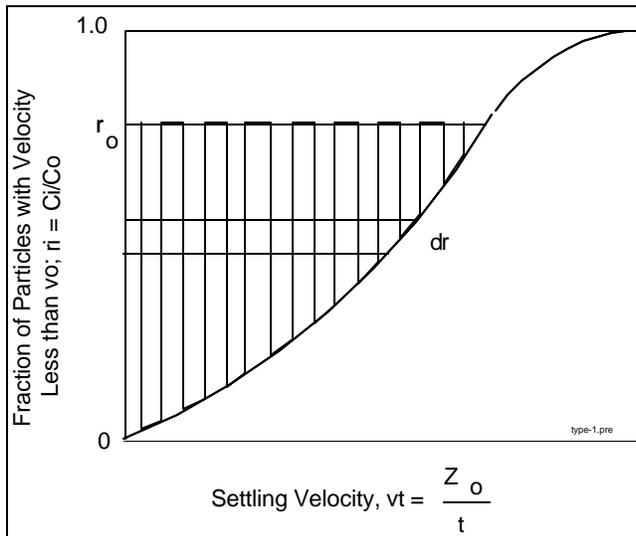


Figure 2: Type 1 Settling Column

6) If the equation relating  $v$  and  $r$  are known, then the area can be found through integration using Eq. 9.



$$R = 1 - r_0 + \int_0^{r_0} \frac{v_t}{v_0} dr \quad (9)$$

where  $R$  is the total fraction removed. However, in most cases this is not possible. Consequently, the relationship is integrated over finite intervals according to Eq. 10.

$$R = (1 - r_0) + \frac{1}{v_0} \sum_0^{r_0} v_t \Delta r \quad (10)$$

**Figure 3: Fraction Remaining**

Example: Settling analysis is run on a Type-1 suspension in a typical 2 m column. Data as follows.

|             |     |     |     |     |     |     |     |     |
|-------------|-----|-----|-----|-----|-----|-----|-----|-----|
| Time, min   | 0   | 60  | 80  | 100 | 130 | 200 | 240 | 420 |
| Conc., mg/L | 300 | 189 | 180 | 168 | 156 | 111 | 78  | 27  |

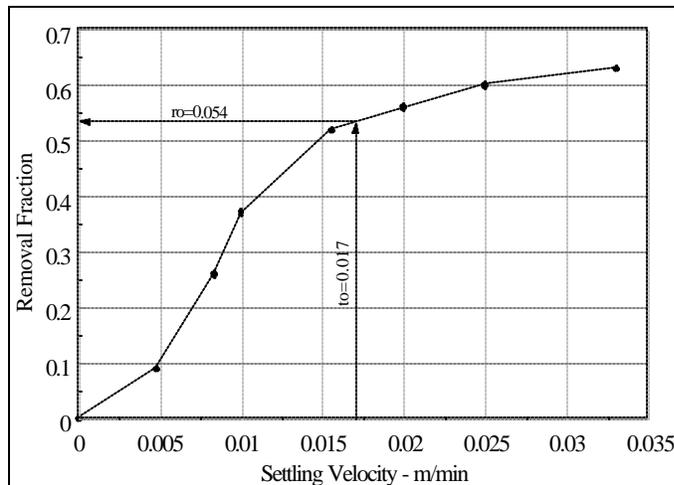
What is the removal efficiency in a settling basin with a loading rate of  $25 \text{ m}^3/\text{m}^2 \cdot \text{d}$  (m/d)?

1. Calculate mass fraction remaining and corresponding settling rates.

|                              |      |      |      |      |      |      |      |
|------------------------------|------|------|------|------|------|------|------|
| Time (min)                   | 60   | 80   | 100  | 130  | 200  | 240  | 420  |
| MF remaining                 | 0.63 | 0.60 | 0.56 | 0.52 | 0.37 | 0.26 | 0.09 |
| $v_t \times 10^{-2}$ (m/min) | 3.3  | 2.5  | 2.0  | 1.55 | 1.0  | 0.83 | 0.48 |

where, mass fraction (MF) remaining =  $C_i/C_0$  and  $v_t = Z_0/t$

- Plot mass fraction remaining vs settling velocity as shown in Figure 4
- Determine velocity ( $v_0$ ), which equals surface loading rate =  $25 \text{ m}^3/\text{m}^2 \cdot \text{d}$  ( $1.7 \times 10^{-2}$  m/min)
- Determine from graph  $r_0 = 54\%$ .
- Integrate curve



**Figure 4: Fraction Removal for Example**

6. Removal efficiency ( $R$ ) =  $1 - r_0 + [\text{Integrated Area}]$

| Element | $\Delta r$ | $v_t \times 10^{-2}$ | $\Delta r \cdot v_t \times 10^{-2}$ |
|---------|------------|----------------------|-------------------------------------|
| 1       | 0.02       | 1.6                  | 0.03                                |
| 2       | 0.15       | 1.25                 | 0.19                                |
| 3       | 0.11       | 0.91                 | 0.10                                |
| 4       | 0.17       | 0.66                 | 0.11                                |
| 5       | 0.09       | 0.24                 | 0.02                                |

Total = 0.45

$$\begin{aligned} \text{Removal} &= (1 - 0.54) + 0.45/1.7 \\ &= 0.46 + 0.26 \\ &= 0.72 \text{ or } 72\% \end{aligned}$$

## USING RESULTS

Primary sedimentation systems have  $\theta_H = 1.5$  to  $2.5$  h, with average overflow rates of  $32$ - $48$  m/d and peak at  $80$  -  $120$  m/d.

|   |                                |   |                                 |
|---|--------------------------------|---|---------------------------------|
| ! | Rectangular (most common)      | ! | circular                        |
| " | depth 3-5 m                    | " | depth 3-5 m                     |
| " | length 15-90 m (30-40 typical) | " | diameter 5-60 m (15-30 typical) |
| " | width 3-24 m (6-10 typical)    |   |                                 |

Example: Use Type 1 Data used in class with  $Q = 2$  m<sup>3</sup>/s with overflow rate of  $25$  m/d.

$$\begin{aligned} A &= Q/25 \\ &= 172,800/25 && \implies \text{assume width} = 10 \text{ m (rectangular)} \\ &= 6912 \text{ m}^2 \end{aligned}$$

$$\text{gives } L = 6912/10 \quad \implies 691 \text{ m (which is too long)}$$

use multiple number of basins; try width =  $10$  and length =  $50$  m

$$\begin{aligned} \text{number of basins} &= 6912/500 \\ &= 13.8 \implies 14 \text{ (always even for rectangular)} \end{aligned}$$

$$\begin{aligned} \text{flow to each} &= 172,800/14 \\ &= 12,343 \text{ m}^3/\text{d} \end{aligned}$$

$$\text{know } t_d = \text{vol}/Q$$

$$\text{assume } t_d = 2.5 \text{ h}$$

$$\text{vol.} = 2.5/24 * 12343 = 1286 \text{ m}^3$$

$$\text{depth} = 1286/10 * 50 = 2.6 \text{ m}$$

## Type-2 Settling

Involves flocculated particles in dilute suspensions. Stokes equations cannot be used because the particles are constantly changing shape and size.

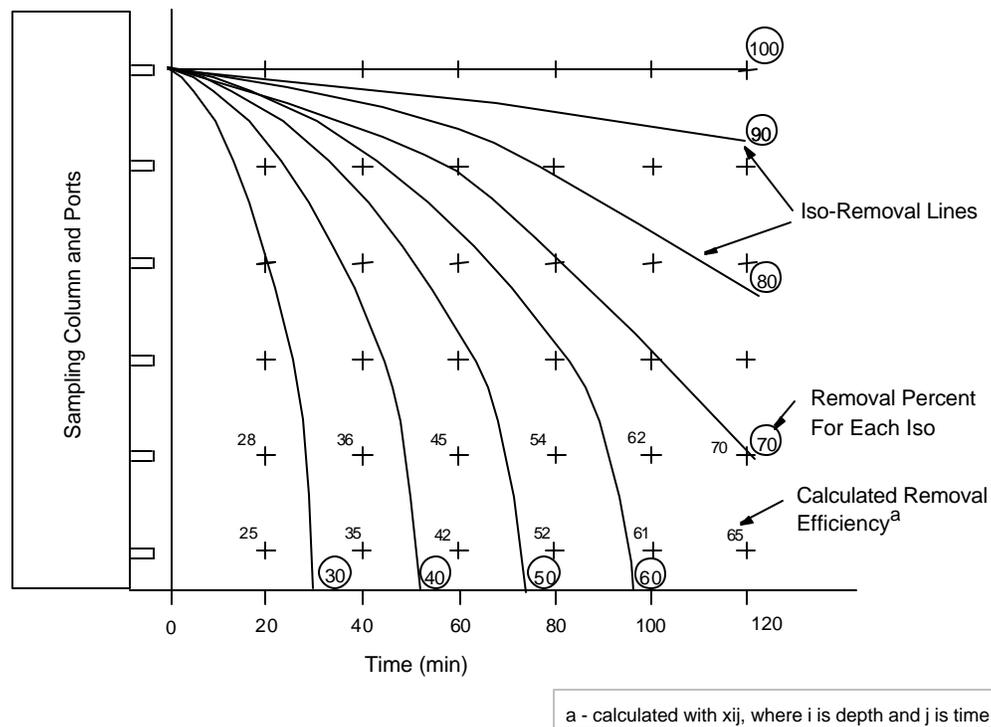
Analysis is similar to the discrete particle suspension, except that the concentrations removed are calculated. This is done by modifying the settling column to have various sample ports as shown. Is a batch test.

$$x_{ij} = (1 - C_i/C_o) \times 100$$

where

$x_{ij}$  = mass fraction percent removed at the  $i$ th depth at the  $j$ th time interval

The sample concentrations are plotted in a contour map showing the iso-removal lines. The slope on any point on the iso-removal line is the instantaneous velocity of the fraction of particles represented by that line. As the velocity increases so does the slope, which is consistent for flocculating suspensions.



**Figure 5: Type II Removal**

Using this method the overall removal percentage can be calculated for any predetermined detention time.

Example - Type II Suspension:

The following table gives the sampling concentrations for a Type II column analysis. The initial solids concentration is 250 mg/L. What is the overall removal efficiency of settling basin 3m deep and a detention time of 1h and 45 min.

| Depth<br>m | Time of sampling, min |     |     |     |     |     |
|------------|-----------------------|-----|-----|-----|-----|-----|
|            | 30                    | 60  | 90  | 120 | 150 | 180 |
| 0.5        | 133                   | 83  | 50  | 38  | 30  | 23  |
| 1.0        | 180                   | 125 | 93  | 65  | 55  | 43  |
| 1.5        | 203                   | 150 | 118 | 93  | 70  | 58  |
| 2.0        | 213                   | 168 | 135 | 110 | 90  | 70  |
| 2.5        | 220                   | 180 | 145 | 123 | 103 | 80  |
| 3.0        | 225                   | 188 | 155 | 133 | 113 | 95  |

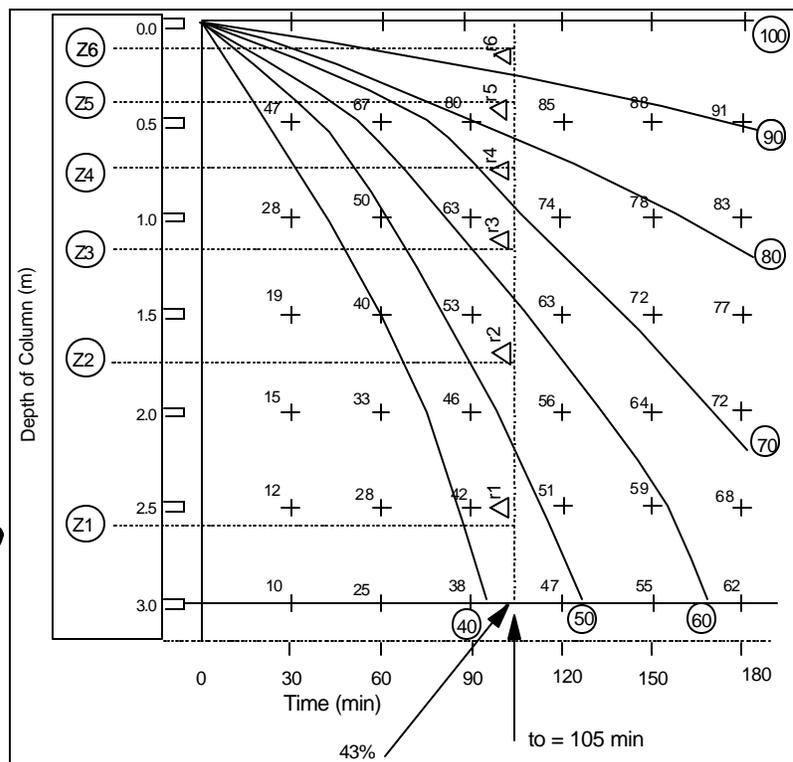
- Determine *removal* rate at each depth and time using  $x_{ij} = (1 - C_i/C_o) \times 100$

| Depth<br>m | Normalized Concentrations - Percent (Time of sampling, min) |    |    |     |     |     |
|------------|---|----|----|-----|-----|-----|
|            | 30  | 60 | 90 | 120 | 150 | 180 |
| 0.5        | 47  | 67 | 80 | 85  | 88  | 91  |
| 1.0        | 28  | 50 | 63 | 74  | 78  | 83  |
| 1.5        | 19  | 40 | 53 | 63  | 72  | 77  |
| 2.0        | 15  | 33 | 46 | 56  | 64  | 72  |
| 2.5        | 12  | 28 |    |     |     |     |
|            | 42  | 51 |    |     |     |     |
| 59         | 68  |    |    |     |     |     |
| 3.0        | 10  | 25 |    |     |     |     |
|            | 38  | 47 |    |     |     |     |
| 55         | 62  |    |    |     |     |     |

- Plot iso-concentration lines as shown in Figure
- Construct vertical line at  $t_o = 105$  min
- Removal efficiency (R) calculated by:

$$R = R_{\text{intercept}} + \frac{1}{H} \sum (Z_i \cdot \Delta R_i)$$

where,  $R_{\text{intercept}} = 43\%$



**Figure 6: Type II Example**

Integrating results in:

| Element | $\Delta R$ | $Z_i$ | $\Delta R \cdot Z_i$ |
|---------|------------|-------|----------------------|
| $r_1$   | 0.07       | 2.55  | 0.179                |
| $r_2$   | 0.1        | 1.73  | 0.173                |
| $r_3$   | 0.1        | 1.13  | 0.113                |
| $r_4$   | 0.1        | 0.72  | 0.072                |
| $r_5$   | 0.1        | 0.39  | 0.039                |
| $r_6$   | 0.1        | 0.12  | 0.012                |
|         |            |       | $\Sigma 0.588$       |

$$R = 0.43 + \frac{1}{3} \Sigma (0.588)$$

$$R = 0.63$$

To improve efficiency, slow down  $v_o$ , calculate  $t_d$  and re-integrate (iterative procedure).

### Hydraulic Characteristics of Settling Basins

The actual flow through characteristics are not the same as assumed for ideal settling basins. Using tracer dyes at the inlet, the tracer will not appear at the same time, i.e. no dispersion like plug flow. Instead the dye appears as shown in Figure 7.

Depth of the settling basins is provided to:

- ▶ Collect sludge without scouring
- ▶ reduce effect of wind velocity
- ▶ reduce agitation of settled sludge under turbulent conditions
- ▶ increase conjunction of flocculent particles
- ▶ reduce short-circuiting
  - ▶ rectangular < outer feed < center feed
- ▶ decrease flow turbulence

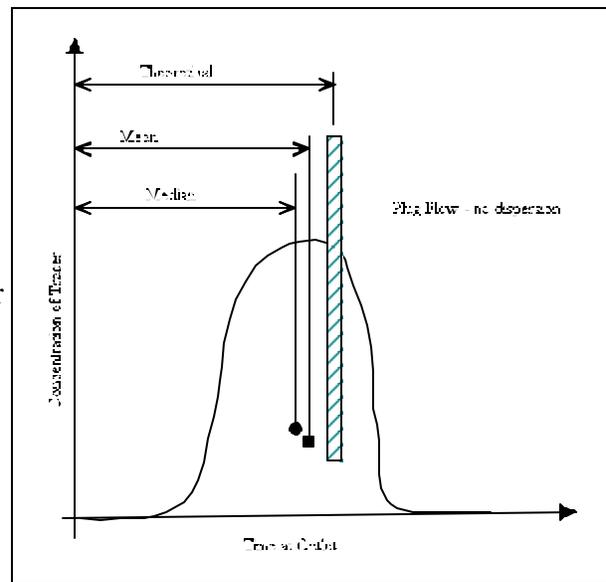


Figure 7: Hydraulic Characteristics